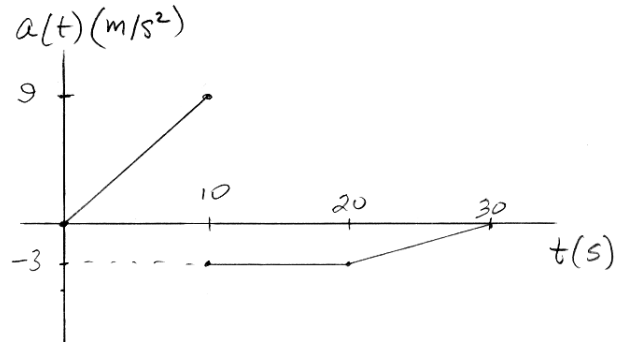


## ME 2580 Dynamics

### Acceleration Profiles – A Second Example

Given: A car has the acceleration profile shown where  $a(t)$  is in (m/sec<sup>2</sup>).

Find:  $v(t)$  and  $s(t)$  the speed and position of the car as functions of time for  $0 \leq t \leq 30$  (sec). Also, find the speed and position of the car when  $t = 30$  (sec). Assume  $v(0) = s(0) = 0$ .



Solution:

$$\underline{0 \leq t \leq 10 \text{ (sec)}}: \quad a(t) = 0.9t = \frac{dv}{dt}, \quad v(t) = \frac{ds}{dt}$$

$$\int_{v_0}^{v(t)} dv = \int_0^t 0.9t \, dt \Rightarrow \boxed{v(t) = 0.45t^2} \Rightarrow v(10) = 45 \text{ (m/sec)}$$

$$\int_{s_0}^{s(t)} ds = \int_0^t 0.45t^2 \, dt \Rightarrow \boxed{s(t) = 0.15t^3} \Rightarrow s(10) = 150 \text{ (m)}$$

$$\underline{10 \leq t \leq 20 \text{ (sec)}}: \quad a(t) = -3 = \frac{dv}{dt}, \quad v(t) = \frac{ds}{dt}$$

$$\int_{v(10)}^{v(t)} dv = \int_{10}^t -3 \, dt \Rightarrow \boxed{v(t) = 75 - 3t} \Rightarrow v(20) = 15 \text{ (m/sec)}$$

$$\int_{s(10)}^{s(t)} ds = \int_{10}^t (75 - 3t) \, dt \Rightarrow \boxed{s(t) = -\frac{3}{2}t^2 + 75t - 450} \Rightarrow s(20) = 450 \text{ (m)}$$

$$\underline{20 \leq t \leq 30 \text{ (sec)}}: \quad a(t) = 0.3t - 9 = \frac{dv}{dt}, \quad v(t) = \frac{ds}{dt}$$

$$\int_{v(20)}^{v(t)} dv = \int_{20}^t (0.3t - 9) \, dt \Rightarrow \boxed{v(t) = 0.15t^2 - 9t + 135} \Rightarrow \boxed{v(30) = 0 \text{ (m/sec)}}$$

$$\int_{s(20)}^{s(t)} ds = \int_{20}^t (0.15t^2 - 9t + 135) \, dt \Rightarrow \boxed{s(t) = 0.05t^3 - 4.5t^2 + 135t - 850}$$

$$\Rightarrow \boxed{s(30) = 500 \text{ (m)}}$$

Sketches of the position, velocity and acceleration functions for  $0 \leq t \leq 30$  (sec) are shown below.

