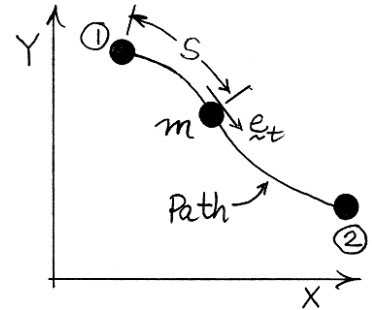


ME 2580 Dynamics

Power and Efficiency

The work done by a force \vec{F} as a particle moves from position 1 to position 2 is

$$U_{1 \rightarrow 2} = \oint \vec{F} \cdot d\vec{r} = \int_{t_1}^{t_2} (\vec{F} \cdot \vec{v}) dt .$$



The **power** generated by \vec{F} at any instant is $P = \vec{F} \cdot \vec{v} = dU/dt$. The average power generated by \vec{F} over an interval of time Δt is $P_{avg} = \Delta U / \Delta t$.

Many mechanical or electro-mechanical systems are used to supply power to (or to do work on) other systems. One common example is the electric motor. These systems must always be supplied a higher level of power than they deliver. The ratio of the power they **deliver** to the power they **received** is defined as the efficiency of the system.

$$\varepsilon = \frac{\text{power delivered}}{\text{power received}} \quad (\text{efficiency of the system})$$

Units:

$$\begin{aligned} 1 \text{ Joule (J)} &= 1 \text{ (N-m)} \\ 1 \text{ Watt (W)} &= 1 \text{ (J/s)} = 1 \text{ (N-m/s)} \\ 1 \text{ Horsepower (HP)} &= 550 \text{ (ft-lb/s)} \end{aligned}$$