

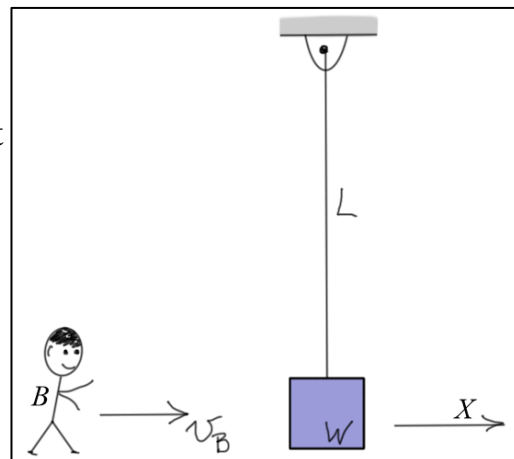
Elementary Dynamics Example #26: (Conservation of Momentum)

Given: $W = 25$ (lb), $W_B = 100$ (lb),
 $v_B = 10$ (ft/s), $L = 20$ (ft)
 boy (B) has velocity v_B as he jumps onto weight
 W and both swing together

Find: h the **maximum height** they swing together

Solution: (**conservation of momentum and energy**)

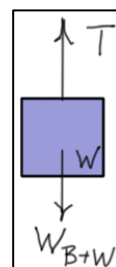
Using **conservation of linear momentum** for the boy and weight in the X direction: (no external forces in the X direction)



$$m_B (v_{Bx})_1 + \underbrace{m_W (v_{Wx})_1}_{\text{zero}} = (m_B + m_W) (v_x)_2$$

Solving:

$$(v_x)_2 = \frac{m_B (v_{Bx})_1}{(m_B + m_W)} = \frac{W_B v_B}{(W_B + W)} = 8 \text{ (ft/s)}$$



Using **conservation of energy**: (from bottom of swing to maximum height)

$$K_2 + \underbrace{V_2}_{\text{zero}} = \underbrace{K_3}_{\text{zero}} + V_3 \quad (\text{assuming datum is at the starting position})$$

where

$$K_2 = \frac{1}{2} \left(\frac{W_B + W}{g} \right) [(v_x)_2]^2 \quad V_3 = (W_B + W)h$$

Solving gives

$$h = \frac{[(v_x)_2]^2}{2g} \approx 0.994 \text{ (ft)}$$