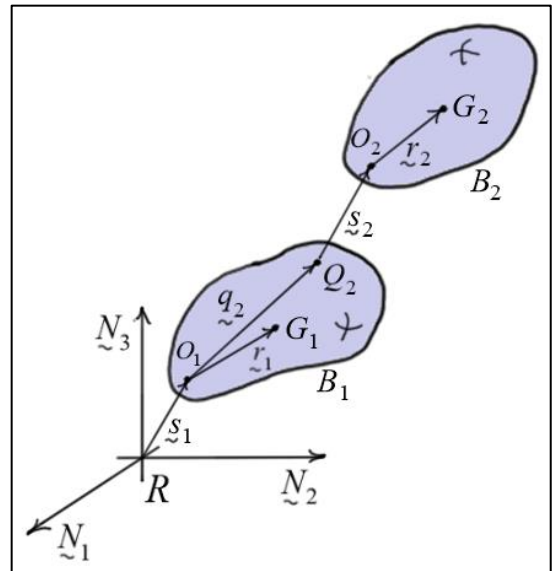
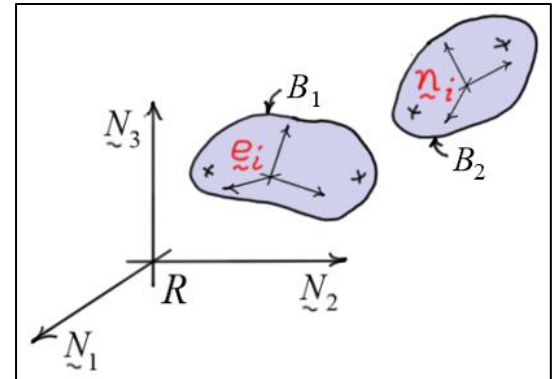


# Multibody Dynamics

## Exercises #3

1. A two-body system is shown in the two figures. The orientations of the bodies are specified relative to the inertial frame  $R$  (*absolute angles*) using 3-2-1 body-fixed rotation sequences. The angles for  $B_1$  and  $B_2$  are  $\theta_{1i}$  and  $\theta_{2i}$  ( $i=1,2,3$ ), respectively. The positions of the bodies are to be specified using *relative coordinates*. The position of body  $B_1$  is given relative to  $R$  and the position of  $B_2$  is given relative to body  $B_1$  as shown in the second figure. The vectors  $\xi_1$  and  $\xi_2$  represent translation vectors of the bodies. The position vectors  $r_1$  and  $q_2$  are fixed in  $B_1$  and the position vector  $r_2$  is fixed in  $B_2$ .



Find  $\{a_{G_2}\}$  the inertial components of the acceleration of  $G_2$  the mass-center of  $B_2$ . Express the results in matrix-vector form using body-fixed angular velocity components. As in Exercises #2, use the components of  $\{\dot{s}_1\}$ ,  $\{\dot{s}'_2\}$ ,  $\{\dot{\theta}_1\}$ , and  $\{\dot{\theta}_2\}$  as the generalized speeds.

2. Given the same set-up as above, find  $\{a_{G_3}\}$  the inertial components of the acceleration of  $G_3$  the mass-center of body 3 of the multibody system shown. Express the results in matrix-vector form using the body-fixed angular velocity components. As in Exercises #2.1, use the components of  $\{\dot{s}_1\}$ ,  $\{\dot{s}'_2\}$ ,  $\{\dot{s}'_3\}$ ,  $\{\dot{\theta}_1\}$ ,  $\{\dot{\theta}_2\}$ , and  $\{\dot{\theta}_3\}$  as the generalized speeds.

